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# X-ray crystal structure determination of the triclinic misfit layer compound $(\mathbf{S n S})_{1.20} \mathrm{TiS}_{2}$ 

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#### Abstract

SnS$)_{2,20} \mathrm{TiS}_{2}$ is a misfit layer compound built of alternately double layers of SnS with distorted rocksalt-type structure and sandwiches of $\mathrm{TiS}_{2}$ slightly distorted compared with those of $1 \mathrm{~T}-\mathrm{TiS}_{2}$. For comparison with other misfit layer compounds the triclinic subsystems are described in centred unit cells: for the SnS part, $a_{1}=5.683(1) \AA, b_{1}=5.832$ (1) $\AA, c_{1}=11.680(5) \AA, \alpha_{1}=95.85(3)^{\circ}, \beta_{1}=94.78(3)^{\circ}, \gamma_{1}=90.03(2)^{\circ}$, the space group is $C \overline{1}$ and $Z=4$; for the TiS 2 part, $a_{2}=3.412(1) \AA, b_{2}=5.835(1) \AA, c_{2}=23.289(3) \AA, \alpha_{2}=$ $95.86(1)^{\circ}, \beta_{2}=90.30(1)^{\circ}, \gamma_{2}=90.01(1)^{\circ}$, the space group is $F 1$ and $Z=4$. In real space, $a_{1}$ and $a_{2}$ as well as $b_{1}$ and $b_{2}$ are parallel while the $c$ axes diverge. In reciprocal space both sublattices have the ( $b^{*}, c^{*}$ ) plane in common. Refinements were performed of the SnS part using 1351 independent reflections ( $R_{F}=0.087$ ) and of the TiS ${ }_{2}$ part using 714 reflections ( $R_{F}=0.080$ ). Each Sn atom is coordinated to five S atoms of the SnS double layer with SnS distances of $2.610(3), 2.866(4), 2.873(4), 2.911(4)$ and $2.976(4) \AA$, and at larger distances to S of $\mathrm{TiS}_{2}$. The Ti-S distances of the distorted $\mathrm{TiS}_{8}$ octahedra with symmetry $\overline{1}$ are $2.417(2)$, $2.429(1)$ and $2.428(1) \AA$. Sn atoms are between rows of sulphur along $a$ of $\mathrm{S}_{\text {of }} \mathrm{TiS}_{2}$. The structural relationship with other misfit layer compounds is discussed.


## 1. Introduction

The discovery (Wiegers et al 1989) of a large number of misfit layer compounds (MS) $\mathrm{TS}_{2}$ ( $\mathrm{M} \equiv \mathrm{Sn}, \mathrm{Pb}$, rare earth metals; $\mathrm{T} \equiv \mathrm{Nb}, \mathrm{Ta}$ ) built of alternately double layers of MS and sandwiches of $\mathrm{TS}_{2}$ with Nb and T a in trigonal prisms of S prompted us to investigate compounds designated as ${ }^{\prime} \mathrm{MTS}_{3}{ }^{\prime}(\mathrm{M} \equiv \mathrm{Pb}$, rare-earth metals; $\mathrm{T} \equiv \mathrm{Ti}, \mathrm{V}, \mathrm{Cr})$ (Takahashi et al 1971,1973 ). The misfit layer character of one of the compounds, i.e. ' $\mathrm{LaCrS}_{3}$ ' was identified by Kato et al (1977) using single-crystal $x$-ray diffraction. The compound was also investigated using electron diffraction (Otera-Diaz et al 1985, Williams and Hyde 1988). Recently Kato (1990) published a reinvestigation of ' $\mathrm{LaCrS}_{3}$ ', based upon the xray data of his previous study. ' $\mathrm{LaCrS}_{3}$ ' with the real composition ( LaS$)_{1.20} \mathrm{CrS}_{2}$ is built of alternate double layers of LaS and sandwiches of $\mathrm{CrS}_{2}$ with Cr in slightly distorted trigonal anti-prismatic coordination by sulphur; both subsystems are described in the space group $C \overline{1}$. Since ' $\mathrm{LaCrS}_{3}$ ' and the title compound ' $\mathrm{SnTiS}_{3}$ ' are structurally related to misfit layer compounds with the transition metal ( $\mathrm{T} \equiv \mathrm{Nb}, \mathrm{Ta}$ ) in trigonal prisms of sulphur, the structures of the latter compounds are briefly reviewed.

For all misfit layer compounds there are two subsystems with compositions MS and $\mathrm{TS}_{2}$, respectively. Each subsystem is characterized by its own unit cell and space group.

Table 1. Crystal data for $(\mathrm{SnS})_{1,20} \mathrm{TiS}_{2}$. Standard deviations are given in parentheses.

|  | SnS part | TiS $_{1}$ part |
| :--- | :---: | :---: |
| Space group no. | $C \overline{1}$ | $F \overline{1}$ |
| $a(\AA)$ | $5.683(1)$ | $3.412(1)$ |
| $b(\AA)$ | $5.832(1)$ | $5.835(1)$ |
| $c(\AA)$ | $11.680(5)$ | $23.289(3)$ |
| $\alpha(\mathrm{deg})$ | $95.85(3)$ | $95.86(1)$ |
| $\beta(\mathrm{deg})$ | $94.78(3)$ | $90.30(1)$ |
| $\gamma(\mathrm{deg})$ | $90.03(3)$ | $90.01(1)$ |
| $V\left(\AA^{3}\right)$ | $383.7(2)$ | $461.2(2)$ |
| 2 | 4 | 4 |

For the misfit layer compounds with $\mathrm{NbS}_{2}$ and $\mathrm{TaS}_{2}$ sandwiches, both MS and $\mathrm{TS}_{2}$ lattices are $C$ or $F$ centred orthorhombic, with corresponding axes parallel. The $c$ axes, $c_{1}$ and $c_{2}$ of MS and $\mathrm{TS}_{2}$, respectively, are perpendicular to the layers. In a recent paper we argued that, when the sandwich $\mathrm{TS}_{2}(\mathrm{~T} \equiv \mathrm{Nb}, \mathrm{Ta})$ is replaced by a sandwich with T in octahedral coordination (as expected for $\mathrm{T}=\mathrm{Ti}, \mathrm{V}, \mathrm{Cr}$ ), monoclinic sublattices result, the monoclinic angle being given by $\sin (\alpha-90)=b / 6 c$, using the same setting of axes (Wiegers et al 1990a). Misfit layer compounds with monoclinic sublattices are observed for $(\mathrm{PbS})_{1.18} \mathrm{TiS}_{2}$ and $(\mathrm{PbS})_{1.13} \mathrm{VS}_{2}$ (Weigers et al 1989, 1990a, van Smaalen 1990, Gotoh et al 1990). Triclinic compounds, such as ' $\mathrm{LaCrS}_{3}$ ', occur when there is an additional shift along the $a$ axes. These shifts, which need not be equal for the two sublattices, are determined by the interaction between subsystems of the same kind. In this paper the structure determination of the triclinic compound $(\mathrm{SnS})_{1.20} \mathrm{TiS}_{2}$ is described.

## 2. Experimental details

A powder sample was prepared from the elements; the ratio of the elements was chosen such as to correspond with the expected ratio in view of $a_{1}$ and $a_{2}$ from respectively the SnS double layer in $(\mathrm{SnS})_{1.17} \mathrm{NbS}_{2}$ (Meetsma et al 1989) and $1 \mathrm{~T}-\mathrm{TiS}_{2}$ (Chianelli et al 1975). The mixture of elements was heated at $800^{\circ} \mathrm{C}$ in an evacuated quartz tube for 7 d. Crystals suitable for electrical transport measurements and single-crystal x-ray diffraction were obtained by vapour transport using chlorine, for which about 1 wt $\%$ $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{PbCl}_{6}$ was used. Crystals grow as thin platelets at the cold part of the gradient of $720-650^{\circ} \mathrm{C}$.

## 3. Structure determination of (SnS) $)_{1.20} \mathrm{TiS}_{2}$

Single-crystal x-ray diffraction was performed on an Enraf-Nonius CAD-4F diffractometer using monochromated Mo $K \bar{\alpha}$ radiation ( $\lambda=0.71073 \AA$ ) and a crystal of approximate dimensions of $0.20 \mathrm{~mm} \times 0.27 \mathrm{~mm} \times 0.006 \mathrm{~mm}$. All reflections could be indexed on two mutually incommensurate triclinic unit cells. For comparison with the orthorhombic and monoclinic misfit layer compounds, centred cells ( $C$ for SnS and $F$ for $\mathrm{TiS}_{2}$ ) are used, with unit-cell dimensions as given in table 1. In real space the $b$ axes are parallel and of equal length while the $a$ axes, being parallel, have a length ratio

(a)
(b)

(c)

Figure 1. The $\mathrm{TiS}_{2}$ sandwich in the orthogonal axes $a_{0}, b_{0}, c_{0}\left(a_{0}\left\|a_{2} ; c_{0}\right\| c_{2}^{*} ; b_{0} \| c_{0} \times a_{0}\right)$. The small and medium circles are Ti and S atoms, respectively. Only the sandwich at $z=0$ is shown. The centres of symmetry are indicated by small crosses. (a) Projection along $c_{0}$ of the S atoms at $z \simeq 0.1$ and the Sn atoms at $z=0$. (b) Projection along $b_{0}$ of the sandwich centred at $z=0$. (c) Projection along $a_{0}$.
$a_{1} / a_{2}=5.683 / 3.412=1.6656$ (standard deviation, 0.0006 ) close to $5 / 3=1.667$. It is not possible to describe the whole structure in a supercell with $a \simeq 3 a_{1} \simeq 5 a_{2}$, because the $c$ axes diverge. The structures of the SnS and $\mathrm{TiS}_{2}$ parts were determined separately. The $0 k l$ reflections were omitted from these refinements because their intensities are determined by both lattices (there is a common ( $b^{*}, c^{*}$ ) reciprocal lattice plane). The 0 kl reflections are used to determine the relative origin of the two sublattices.

Unit-cell dimensions and their standard deviations were for each subsystem determined from the setting angles of a number of reflections in the range $25.95^{\circ}<\theta<27.89^{\circ}$ in four alternative settings (de Boer and Duisenberg 1984). All reflections were measured in one hemisphere up to $\theta=35^{\circ}$. The two reference reflections, $0,4,0$ and $0,0,10$, are common to the two subsystems which has the advantage that the intensities of the two subsystems can be put on the same scale. The intensities were corrected for the scale variation, Lorentz and polarization effects and for absorption using a Gaussian integration method (grid, $10 \times 10 \times 6$ ) (Spek 1983). Standard deviations in the intensities based on counting statistics were increased according to an analysis of the excess variance of the two reference reflections: $\sigma^{2}(I)=\sigma_{\mathrm{cs}}^{2}(I)+(P)^{2}$, where $P$ is the instability constant (McCandlish et al 1975).

For the SnS subsystem refinements were performed in space group $C \overline{1}$ (no. 2 in the International Tables for Crystallography (1983)) with four units SnS in the unit cell. All atoms are at general positions. The midplane of the SnS double layer was taken at $z=\frac{1}{2}$; starting coordinates were deduced from the geometry of the SnS double layer in ( SnS$)_{1.17} \mathrm{NbS}_{2}$ (Meetsma et al 1989). Refinements on $F$ by full-matrix least squares using 1351 reflections with $I \geqslant 2.5 \sigma(I)$, converged at $R_{F}=0.087, w R=0.095, S=4.253$, using units weights.

For the $\mathrm{TiS}_{2}$ part the centric space group $\overline{\mathrm{I}}$ was adopted with Ti at centres of symmetry at $\left(\frac{3}{4}, \frac{1}{4}, 0\right) ;\left(\frac{3}{4}, \frac{3}{4}, 0\right) ;\left(\frac{3}{4}, \frac{1}{4}, \frac{1}{2}\right) ;\left(\frac{1}{4}, \frac{3}{4}, \frac{1}{2}\right)$. There are four formula units $\mathrm{TiS}_{2}$ in the unit cell. It may be noted that there two sets of four symmetry centres in the $F$ centred unit cell. Those given above and one starting with ( $0,0,0$ ) (figure 1). For the $\mathrm{TiS}_{2}$ subsystem, putting the Ti atoms at the centres of either set leads to equivalent descriptions of the same structure. The complete structure will be different when using one or the other set to define the Ti positions. The refinement using the 0 kl reflections showed the choice for the Ti positions given above to be correct. The starting coordinates of $S(2)$ were from a model with Ti in trigonal anti-prismatic coordination. Refinements,
performed by full matrix refinement using 714 reflections ( 0 kl excluded), converged at $R_{F}=0.080, w R=0.096, S=4.310$; unit weights were applied.

From the size of the unit cells in the ( $a, b$ ) plane and the number of SnS and $\mathrm{TiS}_{2}$ formula units per cell, one finds that the composition of the compound is $(\mathrm{SnS})_{t .20} \mathrm{TiS}_{2}$ (i.e. $1.20=2(3.412 / 5.683))$. Because of the common ( $b^{*}, c^{*}$ ) reciprocal plane, the two sublattices have a common projection along [100]. In this projection, $c_{1}$ and $c_{2}$ project along the same line with length $c_{1} \sin \left(\beta_{1}\right)$ for the $\operatorname{SnS}$ lattice and length $c_{2} \sin \left(\beta_{2}\right)=2 c_{1} \sin \left(\beta_{1}\right)$ for the $\mathrm{TiS}_{2}$ lattice. The unit mesh in the projection is given by $b^{\prime \prime}=\frac{1}{2} b_{1}=\frac{1}{2} b_{2}$ and $c^{\prime \prime}=c_{1} \sin \left(\beta_{1}\right)=\left(c_{2} / 2\right) \sin \left(\beta_{2}\right)$. This is also obvious considering the extinctions of the 0 kl reflections, i.e. 0 kl of SnS only present for $k=2 n$ and $0 k l$ of $\mathrm{TiS}_{2}$ only present for $k=2 n$ and $l=2 n$. The two-dimensional space group is $p 2$ (no. 3 of the 17 two-dimensional space groups (International Tables for Crystallograph 1983)). For the refinement using XTAL the three-dimensional space group which describes the symmetry of this projection is $P \overline{1}$. The coordinates of the SnS and $\mathrm{TiS}_{2}$ refinements were transformed to this smaller unit cell. Parameters in the full matrix refinement were the coordinates, the site occupancy factor of Sn and $\mathrm{S}(1)$ (kept equal) and the isotropic thermal parameters of all atoms. The refinement converged to $R_{F}=0.083, w R=0.078$ for 1240 kl reflections, indicating that Ti at $\left(\frac{1}{4}, \frac{1}{4}, 0\right)$, etc, for the $\mathrm{TiS}_{2}$ refinement was the correct choice. The $z$ coordinates are, within standard deviation, equal to those of the subsystem refinements (which are more accurate), taking into account the different unit cells. The composition of the compound obtained from the occupancy of the Sn and $\mathrm{S}(1)$ sites ( $0.592(1))$ is in good agreement with the occupancy, 0.600 , calculated from the lengths of the $a$ axes of the substructures; the same occupancy is calculated from the ratio of the scale factors for the SnS and $\mathrm{TiS}_{2}$ refinements (see the supplementary material $\dagger$ ).

Crystal data and experimental details of the structure determination are compiled in tables 1-4. Final fractional atomic coordinates, sofs and temperature factors are given in table 5 . It may be noted that in this way the structure is completely described by the tables for the SnS and $\mathrm{TiS}_{2}$ parts.

In all our calculations, scattering factors were taken from Cromer and Mann (1968). Anomalous dispersion factors are those given by Cromer and Libermann (1970). All calculations are carried out on the CDC-Cyber 962-31 computer of the University of Groningen with the program packages XTAL (Hall and Stewart 1989) and EUCLID (calculation of geometric data) (Spek 1982).

## 4. Discussion of the structure

$(\mathrm{SnS})_{1.20} \mathrm{TiS}_{2}$ is built of alternately double layers of SnS (approximately a $\{001\}$ slice of SnS with the (hypothetical) rocksalt structure) and sandwiches of $\mathrm{TiS}_{2}$ with Tin distorted octahedral coordination by $S$ as shown in the projection along [100] of both subsystems (figure 2(a)). The symmetry of this projection is that of the two-dimensional space group $p 2$, with unit mesh $b^{\prime \prime}$ and $c^{\prime \prime}$. The figure shows the cell doubled in both directions in order to show the effect of the centring conditions. Since the SnS lattice is $C$ centred, while the $\mathrm{TiS}_{2}$ is $F$ centred, the structure type is designated as $C F$. In this way the relationship with the orthorhombic compound (LaS) ${ }_{1.14} \mathrm{NbS}_{2}$, also of CF type becomes clear (figure $2(b))$. ( LaS$)_{1,20} \mathrm{CrS}_{2}$ which has the $C C$-type structure may be considered as the analogue of $(\mathrm{SnS})_{1.17} \mathrm{NbS}_{2}$ with the orthorhombic CC-type structure.

[^0]Table 2. Data collection for $(\mathrm{SnS})_{1.20} \mathrm{TiS}_{2}$.

|  | SnS part |  | TiS ${ }_{2}$ part |
| :---: | :---: | :---: | :---: |
| Diffractometer | Enraf-Nonius CAD-4F |  |  |
| Radiation | Mo K $\bar{\alpha}$ |  |  |
| Wavelength ( $\AA$ ) | 0.71073 |  |  |
| Monochromator | Graphite |  |  |
| Temperature ( K ) | 295 |  |  |
| Range: minimum, maximum (deg) | 1.76, 35.0 |  | 1.76, 35.0 |
| $\omega-2 \theta \operatorname{scan}$ (deg) | $\Delta \omega=1.30+0.35 \tan \theta$ |  | $\Delta \omega=1.00+0.35 \tan \theta$ |
| Data set | $\begin{aligned} & h,-9 \rightarrow 9 ; k, 0 \rightarrow 9 \\ & \ell,-18 \rightarrow 18 \end{aligned}$ |  | $\begin{aligned} & h,-5 \rightarrow 5 ; k,-9 \rightarrow 0 \\ & l,-36 \rightarrow 36 \end{aligned}$ |
| Crystal-to-receiving-aperture distance (mm) | 173 |  |  |
| Horizontal aperture vertical aperture (mm) | 4.0, 4.5 |  |  |
| Reference reflections, RMS deviation (\%) | 0, 4, 0; 2.20 |  | $\begin{aligned} & 0,4,0 ; 0.59 \\ & 0,0,10 ; 0.73 \end{aligned}$ |
| Instability constant $P$ | 0.0011 |  | 0.0082 |
| Drift correction | 1.000-1.000 |  | 1.000-1.018 |
| Minimum to maximum absorption correction factor | 1.05-2.60 |  | 1.051-2.55 |
| X-ray exposure time (h) | 60.1 |  | 20.5 |
| Total data | 1831 |  | 1105 |
| Unique data | 1117 |  | 410 |

Table 3. Details of the refinement of the SnS and $\mathrm{TiS}_{2}$ parts.

|  | SnS | $\mathrm{TiS}_{2}$ |
| :---: | :---: | :---: |
| Number of reflections: $h \neq 0$ | 1351 | 714 |
| Number of refined parameters | 19 | 16 |
| Final agreement factors |  |  |
| $R_{F}=\Sigma\left(\| \| F_{0}\left\|-\left\|F_{c}\right\|\right\|\right) / \Sigma\left\|F_{0}\right\|$ | 0.087 | 0.080 |
| $w R=\left\{\Sigma\left[w\left(\left\|F_{0}\right\|-\left\|F_{\mathrm{c}}\right\|\right)^{2}\right] / \Sigma w\left\|F_{0}\right\|^{2}\right\}^{1 / 2}$ | 0.095 | 0.096 |
| Weighting scheme | 1 | 1 |
| $S=\left[\Sigma w\left(\left\|F_{\mathrm{o}}\right\|-\left\|F_{\mathrm{c}}\right\|\right)^{2} /(m-n)\right]^{1 / 2}$ where $m$ is the number of observations and $n$ the number of variables | 4.253 | 4.310 |
| Minimum residual density, maximum residual density in final difference Fourier map (electrons $/ \AA^{3}$ ) | -4.6,7.9 | -2.8,2.7 |
| Maximum (shift/ $\sigma$ ) final cycle | $0.25 \times 10^{-2}$ | $0.27 \times 10^{-2}$ |
| Average (shift/ $\sigma$ ) final cycle | $0.68 \times 10^{-3}$ | $0.10 \times 10^{-3}$ |

Using these centred lattices (table 1) one observes that $b_{1}=b_{2}, \gamma_{1}=\gamma_{2}=90^{\circ}$ and $\alpha_{1}=\alpha_{2}, 2 c_{1}=c_{2}$, but $a_{1} \neq a_{2}$ and $\beta_{1} \neq \beta_{2}$. In reciprocal space the sublattices have a common ( $b^{*}, c^{*}$ ) plane. By analysing the latter condition in real space, writing $c_{\mathrm{i}}=$ $c_{\perp}+\lambda_{i} a_{i}+\rho_{i} b_{i}$ in which $c_{\perp}$ is perpendicular to the ( $a, b$ ) plane and using $\gamma_{1}=\gamma_{2}$ (but not necessarily $90^{\circ}$ ) it follows that $a_{1}$ and $a_{2}$ and that $b_{1}$ and $b_{2}$ are parallel, that the interplanar distances $\mathrm{d}_{001}$ are equal, and that the components of $c_{\mathrm{i}}$ along the $b$ axes are equal ( $\rho_{1}=\rho_{2}$ ). It also follows that there will be a slight difference between $\alpha_{1}$ and $\alpha_{2}$,

Table 4. Details of the refinement of the projection along [100] $\left(b^{\prime \prime}=2.916(1) A, c^{\prime \prime}=\right.$ $11.64(3) \AA$; space group, $P \overline{1}$ ).

| Number of reflections, $h=0$ | 124 |
| :--- | :---: |
| Number of refined parameters | 12 |
| Final agreement factors |  |
| $\quad R_{F}=\Sigma\left(\| \| F_{0}\left\|-\left\|F_{\mathrm{c}}\right\|\right\|\right) / \Sigma\left\|F_{0}\right\|$ | 0.083 |
| $w R=\left\{\Sigma\left[w\left(\left\|F_{\mathrm{o}}\right\|-\left\|F_{\mathrm{c}}\right\|\right)^{2}\right] / \Sigma w\left\|F_{\mathrm{o}}\right\|^{21}\right\}^{1 / 2}$ | 0.078 |
| Weighting scheme | 1 |
| $S=\left[\Sigma w\left(\left\|F_{\mathrm{o}}\right\|-\left\|F_{\mathrm{c}}\right\|\right)^{2} /(m-n)\right]^{1 / 2}$ where $m$ is the number of observations and |  |
| $\quad n$ the number of variables | 1.773 |
| Residual electron density in final difference Fourier map (electrons $\left./ \AA^{3}\right)$ | $-1.14,1.29$ |
| Maximum (shift $/ \sigma$ ) final cycle | $0.94 \times 10^{-1}$ |
| Average (shift $/ \sigma$ ) final cycle | $0.17 \times 10^{-1}$ |

given by $\cos \left(\alpha_{\mathrm{i}}\right)=\rho_{\mathrm{i}} b_{\mathrm{i}} / c_{\mathrm{i}}$. The calculated difference between $\alpha_{1}$ and $\alpha_{2}$ of $0.01^{\circ}$ is less than the estimated standard deviation. The angles $\beta_{\mathrm{i}}$, which are not equal, are determined by $\lambda_{i} a_{\mathrm{i}}$, i.e. $\cos \left(\beta_{\mathrm{i}}\right)=\lambda_{\mathrm{i}} a_{\mathrm{i}} / c_{\mathrm{i}}$. Because of the incommensurate character of the complete structure along the $a$ axes, the energy due to nearest-neighbour interaction of layers will not change when $\lambda_{i}$ is changed. The constants $\lambda_{1}$ are therefore determined by the interaction between layers of the same kind and therefore one does not expect a relation between $\lambda_{1}$ and $\lambda_{2}$. For $\lambda_{1}=\lambda_{2}=0, \beta_{1}=\beta_{2}=90^{\circ}$, the two sublattices are monoclinic and corresponding axes are parallel. Monoclinic lattices with $\beta_{i}=\gamma_{i}=90^{\circ}$ are observed for ' $\mathrm{PbTiS}_{3}$ ' and ' $\mathrm{PbVS}_{3}$ ' (Wiegers et al 1989, 1990a, van Smaalen et al 1990, Gotoh et al 1990).

That the subsystems of all misfit layer compounds (including those with $\mathrm{T} \equiv \mathrm{Nb}$ and Ta) have a common ( $b^{*}, c^{*}$ ) reciprocal plane seems to be a necessary condition for their existence. A common $c^{*}$ is a consequence that layers cannot intersect. A common ( $b^{*}, c^{*}$ ) plane means that the $a$ axes of the subsystems must be parallel, which in turn means that [001] is the direction along which the bonding interaction of alternate layers takes place. A common ( $b^{*}, c^{*}$ ) plane occurs also for a system of $a b$ axes with the $a$ axes parallel and $b$ axes such that $b_{1} \sin \left(\gamma_{1}\right)=b_{2} \sin \left(\gamma_{2}\right)$, which means that a rectangular shape of the ( $a, b$ ) planes and $b_{1}=b_{2}$ as observed for all compounds is not essential in having a common ( $b^{*}, c^{*}$ ) plane.

In the projection of the substructures along [100], $c_{1}$ and $c_{2}$ project with length $c_{1} \sin \left(\beta_{1}\right)=c_{2} \sin \left(\beta_{2}\right)$ along the same line, the angle between $b$ and the projected $c_{1}$ and $c_{2}$ being almost equal: $\alpha_{1}=\alpha_{2}$ (figure $2(a)$ ).

The structure of the SnS double layer is shown more clearly in figure 3 . Each Sn atom is coordinated by five S atoms within the same double layer and at larger distances by two or three S atoms of the $\mathrm{TiS}_{2}$ subsystem (indicated by broken and full lines, respectively, in figure 2(a)). It is seen that, compared with an $\{001\}$ slice of SnS with rocksalt structure (hypthetical, since SnS adopts a different structure), the SnS double layer is corrugated with Sn atoms on the outside. The Sn bond to the apex S atom of the SnS double layer, in projection almost perpendicular to the $b$ axis, is much shorter (2.610(3) $\AA$ ), than the other four $\mathrm{Sn}-\mathrm{S}$ distances which are $2.866(4), 2.873(4), 2.911(4)$ and $2.976(4) \AA$ (table6). The same phenomenon is observed for the SnS double layer in $(\mathrm{SnS})_{1,17} \mathrm{NbS}_{2}$ (Meetsma et al 1989).

The Sn atoms fall in between rows of sulphur in $\mathrm{TiS}_{2}$ along $a$, making the total number of coordinating $S$ atoms $5+2$ or $5+3$, depending on the actual position along the misfit
Table 5. Atomic positions and temperature factors of $(\mathrm{SnS})_{12} \mathrm{TiS}_{2}$. Values of the fractional coordinates of the SnS and $\mathrm{TiS}_{2}$ parts are with respect to the unit cell defined in table 1. Estimated standard deviations are given in parentheses. $U_{\mathrm{cq}}=\left\{\Sigma_{i} \Sigma_{j} U_{i j} a_{i}^{*} a_{i}^{*} a_{j} \cdot a_{j}\right.$. The thermal vibration amplitudes $\left(\AA^{2}\right)$ are $F(h)=F_{\mathrm{o}}(h)$ $\exp \left(-2 \pi^{2} \Sigma_{i=1}^{3} \Sigma_{j=1}^{3} h_{i} h_{j} a_{i}^{*} a_{j}^{*} U_{i j}\right)$.

|  | $x$ | $y$ | $z$ | $U_{\text {eq }}\left(\AA^{2}\right)$ | $\begin{aligned} & U_{11} \\ & \left(\AA^{2}\right) \end{aligned}$ | $\begin{aligned} & U_{22} \\ & \left(\AA^{2}\right) \end{aligned}$ | $\begin{aligned} & U_{33} \\ & \left(\AA^{2}\right) \end{aligned}$ | $\begin{aligned} & U_{23} \\ & \left(\AA^{2}\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Sn}(1)$ | -0.0225(1) | $-0.28060(2)$ | $0.37000(7)$ | 0.0228(2) | 0.0210(2) | 0.0160(2) | 0.0084(1) | $0.0016(5)$ |
| S(1) | 0.0160(6) | -0.2320(6) | 0.5954 (3) | 0.0289(8) | $0.0171(6)$ | 0.0108(8) | 0.0079(5) | 0.004(1) |
| $\mathrm{Ti}(1)$ | $\frac{1}{4}$ | 4 | 0.0 | 0.0122(4) | 0.0141(6) | $0.0014(6)$ | $0.0005(5)$ | $0.00000(0)$ |
| S(2) | 0.2480(4) | 0.5587(2) | 0.06175(6) | 0.0083(3) | 0.016(1) | 0.004(1) | 0.002(1) | 0.001(1) |
|  | $x^{\prime \prime}$ | $y^{\prime \prime}$ | $z^{\prime \prime}$ | $\stackrel{\text { SOF }}{1}$ | $\begin{aligned} & U_{\text {iso }} \\ & \left(\AA^{2}\right) \end{aligned}$ |  |  |  |
| Common part (coordinates a unit cell with $b^{\prime \prime}=2.883(1) \AA, c^{\prime \prime}=11.41(1) \AA$ ) |  |  |  |  |  |  |  |  |
| $\mathrm{Sn}(1)$ | - | -0.561(1) | $0.3704(3)$ | 0.592(1) | 0.026(1) |  |  |  |
| S(1) | - | -0.466(5) | 0.592(1) | 0.592(1) | 0.029(4) |  |  |  |
| Ti(1) | - | $\frac{1}{2}$ | 0 | 1.0 | 0.011(1) |  |  |  |
| S(2) | - | 0.119(2) | -0.1236(4) | 1.0 | 0.009(1) |  |  |  |



Figure 2. (a) The structure of the common projection (along [100]) of ( SnS$)_{1.20} \mathrm{TiS}_{2}$. (b) The corresponding projection of $(\mathrm{LaS})_{1.14} \mathrm{NbS}_{2}$. The centring ( $C$ for SnS ( LaS ) and $F$ for $\mathrm{TiS}_{2}\left(\mathrm{NbS}_{2}\right)$ ) is demonstrated using open and shaded circles for atoms of the same type, $\frac{1}{2} a$ apart. For $(\mathrm{SnS})_{1.20} \mathrm{TiS}_{2}$ the c axes of the subsystems project onto the same vector.


Figure 3. The structure of the SnS double layer of $(\mathrm{SnS})_{1.20} \mathrm{TiS}_{2}$ in orthogonal axes $a_{0}$, $b_{0}, c_{0}\left(a_{0}\left\|a_{1} ; c_{0}\right\| \boldsymbol{c}_{1}^{*} ; b_{0} \| c_{0} \times a_{0}\right)$. The small and medium circles are $S n$ and $S$ atoms, respectively. The centres of symmetry are indicated by small crosses. (a) Projection along $c_{0}$; only the lower half of the double layer is shown. (b) Projection along $b_{0}$.

Table 6. Interatomic distances and angles in $\left(\mathrm{SnS}_{1.20} \mathrm{TiS}_{2}\right.$. The numbering of atoms refers to figures 1 and 3 .

|  | Interatomic distance ( $\AA$ ) |  | Angle (deg) |  | Angle <br> (deg) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Sn}-\mathrm{S}(1 \mathrm{a})$ | 2.866(4) | S(1a)-Sn-S(1b) | 163.9(1) | S(1b)-Sn-S(1d) | 88.3(1) |
| $\mathrm{Sn}-\mathrm{S}(16)$ | 2.873(4) | S(1c)-Sn-S(1d) | 164.4(1) | S(1a)-Sn-S(1e) | 82.0(1) |
| $\mathrm{Sn}-\mathrm{S}(1 \mathrm{c})$ | $2.911(4)$ | S(1a)-Sn-S(1c) | 89.6(1) | S(1b)-Sn-S(1e) | 82.0(1) |
| Sn-S(1d) | $2.976(4)$ | $\mathbf{S}(1 \mathrm{a})-\mathbf{S n}-\mathrm{S}(1 . d)$ | 88.3(1) | $\mathrm{S}(1 \mathrm{c})-\mathrm{Sn}-\mathrm{S}(1 \mathrm{e})$ | 82.4(1) |
| Sn-S(1e) | 2.6109(3) | $S(1 b)-S n-S(1 c)$ | 89.5(1) | S(1d)-Sn-S(1e) | 81.9(1) |
| Ti-S(2a) | 2.417(2) | S(2a)-Ti-S(2b) | 88.46(4) |  |  |
| Ti-S(2b) | 2.428(1) | S(2a)-Ti-S(2c) | 88.45 (4) |  |  |
| Ti-S(2c) | 2.429(1) | S(2b)-Ti-S(2c) | 89.26(5) |  |  |

$a$ direction. In the case of an undistorted $\mathrm{TiS}_{2}$ sandwich the rows of S above and below Ti are displaced over ( $\frac{1}{6}$ ) $b$; when rows of $S$ of the Sn double layer have no displacement along $b$, then $\rho_{i}=\frac{1}{6}$, and the angles $\alpha_{i}$, given by $\cos \left(\alpha_{i}\right)=\rho_{i} b_{i} / c_{i}$ are $94.77^{\circ}(\mathrm{SnS})$ and $94.79^{\circ}\left(\mathrm{TiS}_{2}\right)$. The difference with the observed values is caused by the distortion of SnS and $\mathrm{TiS}_{2}$.

The $\mathrm{TiS}_{2}$ sandwich is slightly distorted compared with $1 \mathrm{~T}-\mathrm{TiS}_{2}$. The Ti-S distances and angles $\mathrm{S}-\mathrm{Ti}-\mathrm{S}$ in table 6 show that the symmetry of a $\mathrm{TiS}_{6}$ polyhedron is $2 / m$ (note
that the space group of $1 \mathrm{~T}-\mathrm{TiS}_{2}$ in an orthohexagonal cell is $C 2 / m$ ). The Ti-S distances (table 6), with an average of $2.425 \AA$, are close to those observed in 1T-TiS $2,2.4279 \AA$ (Chianelli et al 1975).

## 5. Superspace group symmetry

Analogous to the discussion for the orthorhombic misfit layer compounds (Wiegers et al 1990b, van Smaalen 1989) the superspace group defines a relation between the subsystem space groups. Here it shows that both subsystems must be centrosymmetric (as found in this study) or both subsystems are acentric. Furthermore, the superspace group gives information about the centring of the individual unit cells. The combination $C F$ as found for ( SnS$)_{1.20} \mathrm{TiS}_{2}$ is possible; however, a loss of centring in one subsystem (e.g. $C \rightarrow P$ ) implies the loss of a related centring in the other subsystem. The $(3+1)$ dimensional superspace group which characterizes the complete structure of $(\mathrm{SnS})_{1,20} \mathrm{TiS}_{2}$ is $P: F \overline{1}: \overline{1}(\alpha \beta \gamma)$, the centring representing
$\left.\begin{array}{cccc}\left(\frac{1}{2}\right. & \frac{1}{2} & 0 & \frac{1}{2}\end{array}\right)$.

The reciprocal lattice vectors of the two subsystems $\mathrm{SnS}(\nu=1)$ and $\mathrm{TiS}_{2}(\nu=2)$, $a_{\nu j}^{*}(\nu=1,2 ; j=1,2,3)$, are as follows associated with the four reciprocal lattice vectors $a_{i}^{*}(i=1,2,3,4)$ in $(3+1)$-dimensional superspace:

$$
\left[\begin{array}{l}
a_{\nu 1}^{*} \\
a_{\nu 2}^{*} \\
a_{\nu 3}^{*}
\end{array}\right]=Z^{v}\left[\begin{array}{l}
a_{1}^{*} \\
a_{2}^{*} \\
a_{3}^{*} \\
a_{4}^{*}
\end{array}\right]
$$

with

$$
Z^{1}=\left[\begin{array}{llll}
0 & 0 & 0 & 1 \\
0 & 1 & 0 & 0 \\
0 & 0 & 2 & 0
\end{array}\right] \quad Z^{2}=\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & \theta \\
0 & 0 & 1 & 0
\end{array}\right]
$$

Not yet discussed is the mutual modulation of the two sublattices which gives rise to satellite reflections with indices $h k l m(h, m \neq 0)$ using the four reciprocal lattice vectors given above. Satellites due to this modulation are visible by electron diffraction (Wiegers et al 1989) but they are too weak to be observed on Weissenberg photographs taken with $\mathrm{CuK} \alpha$ radiation. In the average structure as obtained by our structure determinations (see, e.g., the discussion given for (LaS) ${ }_{1.14} \mathrm{NbS}_{2}$ and $(\mathrm{PbS})_{1.14} \mathrm{NbS}_{2}$ by Wiegers et al (1990b)), the modulation is visible in the temperature factors of the atoms. The rather
high $R$-factors of our structure determination may arise because the mutual modulation is not taken into account.

## 6. Phase relationships

The compounds ' $\mathrm{SnTiS}_{3}$ ' and ' $\mathrm{SnTi}_{2} \mathrm{~S}_{5}$ ' were reported by Guemas et al (1988). The unitcell dimensions deduced from Weissenberg photographs of poorly crystallized ' $\mathrm{SnTiS}_{3}$ ' (orthorhombic with unit-cell dimensions $a=23.3 \AA, b=5.79 \AA$ and $c=23.3 \AA$ ) indicate that their compound ' $\mathrm{SnTiS}_{3}$ ' is essentially the triclinic compound of our study. The compound ' $\mathrm{SnTi}_{2} \mathrm{~S}_{5}$ ' with $c=35.13 \AA$ is presumably a stacking of one SnS double layer followed by two $\mathrm{TiS}_{2}$ sandwiches. In the mixed-valence compound $\mathrm{Sn}_{2} \mathrm{~S}_{3}$ with $\mathrm{Sn}(\mathrm{II})$ and $\mathrm{Sn}(\mathrm{IV})$, part of $\mathrm{Sn}(\mathrm{IV})$ can be replaced by $\mathrm{Ti}(\mathrm{IV})$, forming a compound $\mathrm{Sn}_{1.2} \mathrm{Ti}_{0.8} \mathrm{~S}_{3}$ (Gressier et al 1987).

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[^0]:    $\dagger$ The supplementary material (lists of $F_{\mathrm{o}}, F_{\mathrm{c}}$ and $\sigma(F)$ ) can be obtained from the authors.

